

## ON $\delta$ -SEMIPERFECT MODULES

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(based on a joint work with Hau Xuan Nguyen and Yiqiang Zhou [3])

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ABSTRACT. A submodule  $N$  of a module  $M$  is  $\delta$ -small in  $M$  if  $N + X \neq M$  for any proper submodule  $X$  of  $M$  with  $M/X$  singular ([4]). A projective  $\delta$ -cover of a module  $M$  is a projective module  $P$  with an epimorphism to  $M$  whose kernel is  $\delta$ -small in  $P$ . A module  $M$  is called  $\delta$ -semiperfect if every factor module of  $M$  has a projective  $\delta$ -cover. In this presentation, I will mention various properties, including a structure theorem and several characterizations, for  $\delta$ -semiperfect modules. Our proofs can be adapted to generalize several results of Mares ([1]) and Nicholson ([2]) from projective semiperfect modules to arbitrary semiperfect modules.

### References

- [1] E. A. MARES:, *Semi-perfect modules*, Math. Z. **82** (1963) , 347360.
- [2] W. K. NICHOLSON: *On semiperfect modules*, Canad. Math. Bull. **18** (1) (1975), 77-80.
- [3] H. X. NGUYEN, M. T. KOŞAN AND Y. ZHOU: *On  $\delta$ -Semiperfect Modules*, Commun. Algebra, in press.
- [4] Y. ZHOU: *Generalizations of perfect, semiperfect and semiregular rings*, Algebra Colloq. **7** (3) (2000), 305-318.

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